

Extension-based semantics:

S is *conflict-free* (CF) if there are no $a, b \in S$ such that $(a, b) \in R$.

S *defends* a if for each $b \in A$, if $(b, a) \in R$ then b is attacked by S .

S is *admissible* if it is CF and each argument of S is defended by S .

S is a *complete* extension if it is admissible and every argument defended by S belongs to S .

S is a *preferred* extension if it is maximal (for \subseteq) admissible set.

S is a *stable* extension if it is CF and attacks all the arguments that do not belong to S .

S is a *grounded* extension if it is the min. (for \subseteq) complete extension.

Principles for ranking-based semantics:

S satisfies *anonymity* iff, for any two WAGs $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$ and $G' = \langle \mathcal{A}', w', \mathcal{R}' \rangle$, for any isomorphism f from G to G' , the following property holds: $\forall a \in \mathcal{A}, \text{Deg}_G^S(a) = \text{Deg}_{G'}^S(f(a))$.

S satisfies *independence* iff, for any two WAGs $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$ and $G' = \langle \mathcal{A}', w', \mathcal{R}' \rangle$ s.t. $\mathcal{A} \cap \mathcal{A}' = \emptyset$, the following holds: $\forall a \in \mathcal{A}, \text{Deg}_G^S(a) = \text{Deg}_{G \oplus G'}^S(a)$.

S satisfies *directionality* iff, for any two WAGs $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $G' = \langle \mathcal{A}, w, \mathcal{R}' \rangle$ s.t. $\mathcal{R}' = \mathcal{R} \cup \{(a, b)\}$, it holds that: $\forall x \in \mathcal{A}$, if there is no path from b to x , then $\text{Deg}_G^S(x) = \text{Deg}_{G'}^S(x)$.

S satisfies *neutrality* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a, b \in \mathcal{A}$, if i) $w(a) = w(b)$, and ii) $\text{Att}_G(b) = \text{Att}_G(a) \cup \{x\}$ with $x \in \mathcal{A} \setminus \text{Att}_G(a)$ and $\text{Deg}_G^S(x) = 0$, then $\text{Deg}_G^S(a) = \text{Deg}_G^S(b)$.

S satisfies *equivalence* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a, b \in \mathcal{A}$, if i) $w(a) = w(b)$, and ii) there exists a bijective function f from $\text{Att}_G(a)$ to $\text{Att}_G(b)$ s.t. $\forall x \in \text{Att}_G(a)$, $\text{Deg}_G^S(x) = \text{Deg}_G^S(f(x))$, then $\text{Deg}_G^S(a) = \text{Deg}_G^S(b)$.

S satisfies *maximality* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a \in \mathcal{A}$, if $\text{Att}_G(a) = \emptyset$, then $\text{Deg}_G^S(a) = w(a)$.

S satisfies *weakening* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a \in \mathcal{A}$, if i) $w(a) > 0$, and ii) $\exists b \in \text{Att}_G(a)$ s.t. $\text{Deg}_G^S(b) > 0$, then $\text{Deg}_G^S(a) < w(a)$.

S satisfies *counting* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a, b \in \mathcal{A}$, if i) $w(a) = w(b)$, ii) $\text{Deg}_G^S(a) > 0$, and iii) $\text{Att}_G(b) = \text{Att}_G(a) \cup \{y\}$ with $y \in \mathcal{A} \setminus \text{Att}_G(a)$ and $\text{Deg}_G^S(y) > 0$, then $\text{Deg}_G^S(a) > \text{Deg}_G^S(b)$.

S satisfies *weakening soundness* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a \in \mathcal{A}$ s.t. $w(a) > 0$, if $\text{Deg}_G^S(a) < w(a)$,

then $\exists b \in \text{Att}_G(a)$ s.t. $\text{Deg}_G^S(b) > 0$.

S satisfies *reinforcement* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a, b \in \mathcal{A}$, if i) $w(a) = w(b)$, ii) $\text{Deg}_G^S(a) > 0$ or $\text{Deg}_G^S(b) > 0$, iii) $\text{Att}_G(a) \setminus \text{Att}_G(b) = \{x\}$, iv) $\text{Att}_G(b) \setminus \text{Att}_G(a) = \{y\}$, and v) $\text{Deg}_G^S(y) > \text{Deg}_G^S(x)$, then $\text{Deg}_G^S(a) > \text{Deg}_G^S(b)$.

S satisfies *resilience* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a \in \mathcal{A}$, if $w(a) > 0$, then $\text{Deg}_G^S(a) > 0$.

S satisfies *proportionality* iff, for any WAG $G = \langle \mathcal{A}, w, \mathcal{R} \rangle$, $\forall a, b \in \mathcal{A}$ s.t. i) $\text{Att}_G(a) = \text{Att}_G(b)$, ii) $w(a) > w(b)$, and iii) $\text{Deg}_G^S(a) > 0$ or $\text{Deg}_G^S(b) > 0$, then $\text{Deg}_G^S(a) > \text{Deg}_G^S(b)$.

Weighted h -categorizer:

$$f_h^i(a) = \begin{cases} w(a) & \text{if } i = 0; \\ \frac{w(a)}{1 + \sum_{b_i \in \text{Att}(a)} f_h^{i-1}(b_i)} & \text{otherwise.} \end{cases}$$

TB semantics:

$$f_i^{TB}(a) = \frac{1}{2} f_{i-1}^{TB}(a) + \frac{1}{2} \min[w(a), 1 - \max_{b \in \text{Att}(a)} f_{i-1}^{TB}(b)]$$

$$\text{with } f_0^{TB}(a) = w(a)$$

Simple product semantics (SAF):

$$\text{Deg}(a)_G^{SAF} = \tau(a) \cdot (1 - (\text{Deg}_G^{SAF}(b_1) \curlywedge \dots \curlywedge \text{Deg}_G^{SAF}(b_n)))$$

where, $\text{Att}(a) = \{b_1 \dots b_n\}$, and $x \curlywedge y = x + y - x \cdot y$

DF-Quad:

$$\text{Deg}(a) = w(a) \cdot \prod_{b \in \text{Att}(a)} (1 - \text{Deg}(b))$$

Translating an extension-based semantics into a ranking-based semantics: (1) $a \succeq b$ iff $w(a) \geq w(b)$. (2) Obtain a new attack relation \mathcal{R}' by deleting the attacks from a to b s.t. $b \succ a$. (3) Apply Dung's semantics on $\langle \mathcal{A}, \mathcal{R}' \rangle$. Then: if a belongs to all extensions, $\text{Deg}(a) = 1$; else, if a belongs to at least one extension, $\text{Deg}(a) = 0.5$; else, if a is not attacked by any extension, $\text{Deg}(a) = 0.3$; else, $\text{Deg}(a) = 0$.